Electronic Instrumentation for Measurement

Introduction

EIM

Contents

- Introduction
- □ DAC ADC converters
- Digital scope (oscilloscope)
- Digital voltmeter
- Z-meter
- Spectrum analyzer
- Direct digital synthesizer

Measurement = process of comparing the unknown quantity with an accepted standard quantity (u.m.);

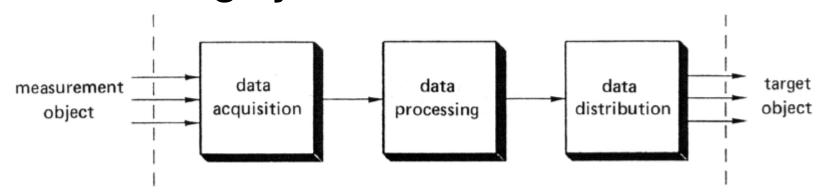
Measuring system aims:

- to obtain information about a physical process;
- to find appropriate ways of presenting that information to an observer or to other technical systems;

Measuring system functions:

- data acquisition acquiring information about the object to be measured and converting into electrical measurement data;
- data processing processing, selecting or manipulating measured data;
- data distribution supplying of measured data to the target object.

Measuring system functions:

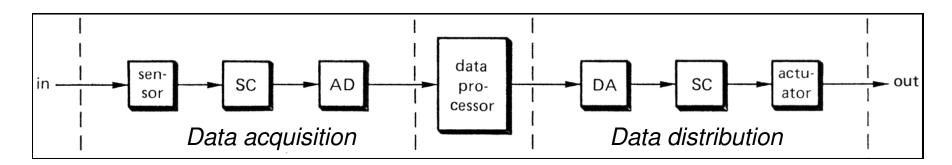


Data acquisition:

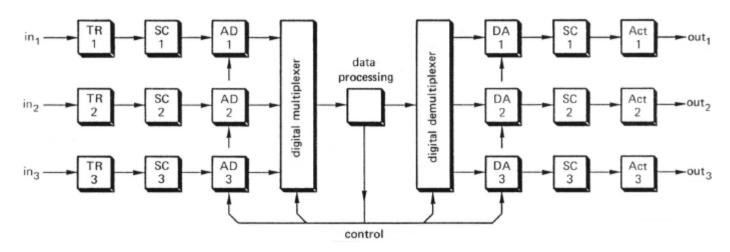
- Sensor or transducer produces an electrical analog signal (including conversion into electrical measurement data of nonelectrical information);
- Signal conditioning: amplification, filtering, modulation, demodulation, non-linear operations of electrical signal;
- AD-converter: sample & hold, quantization, binary encoder;

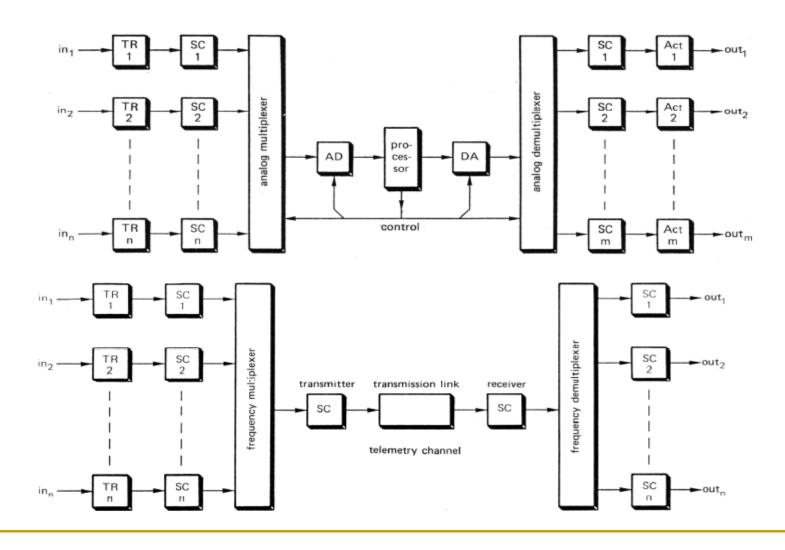
Data distribution

- DA converter (optional);
- Signal conditioning (optional) for DAC output signal adapting to actuator input: antialiasing filtering, amplification, filtering, nonlinear operations;
- Actuator (effector) transforms the electrical signal into the desired non-electric form. Type of actuator functions: indicating (on display), storing (memory, CD, printer, etc), controlling (valve, heating element, electrical dive, etc);



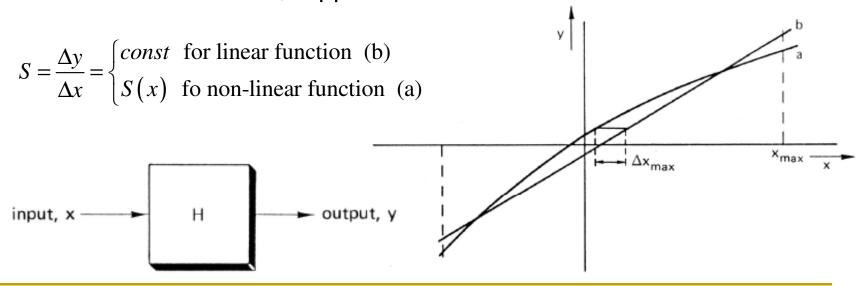
- Multi-channel measuring system
 - central processor and digital multiplexer (time division) fast data processing, slow ADC, DAC;
 - centralized processor and AD and DA-converters and analog multiplexer (time division) - fast data processing, ADC, DAC;
 - system with frequency multiplexing (frequency division) telemetry;





Measuring system specifications

- measurement range (0 100V, 0-2A, etc) the region between the specified maximum value (Full-scale FS) and minimum value (usually 0) where the system can be used for measurement;
- resolution the smallest detectable change in input quantity;
- sensitivity ratio between the output variation (y) to the input variation (x) that causes that output change (linear / nonlinear function: saturation, clipping, dead zone);



- Measuring system specifications (cont'd)
 - □ bandwidth the frequency span between frequencies $(f_i f_s)$ where the system output has dropped to half from the nominal value;
 - accuracy how precise the measured value is (compared to the real value) complementary to inaccuracy);
 - \square input impedance (1M Ω ||27pF);
 - environmental operating range:
 - supply voltage (220V- 50Hz, 110V-60Hz, etc);
 - the environmental conditions: operational temperature (−10°C to 40°C), storage temperature (-20°C to 85°C), humidity (10% to 95%), altitude (0m to 6000m), etc.
 - other parameters : load (>20Ω);
 - reliability of the system (failure rate λ(t) or the mean-timeto-failure MTTF);

Course 1 - Introduction EIM

Accuracy of measurement

Classical way-error of measurement (instant or maximum)

absolute error
$$e_X = X_m - X_{ad}$$
 where $\begin{cases} X_m \text{ measured value} \\ X_{ad} \end{cases}$ true value

$$\Box$$
 accuracy $A_x = 1 - \varepsilon_y$

accuracy
$$A_x = 1 - \mathcal{E}_X$$
 error propagation
$$e_Y = \sum_{k=1}^N \left| \frac{\partial F(X_1, X_2, ... X_N)}{\partial X_k} \cdot e_{X_k} \right|$$

$$\varepsilon_{Y} = \frac{1}{F(X_{1}, X_{2}, ... X_{N})} \cdot \sum_{k=1}^{N} \left| \frac{\partial F(X_{1}, X_{2}, ... X_{N})}{\partial X_{k}} \cdot X_{k} \cdot \varepsilon_{X_{k}} \right|$$

Accuracy of measurement

Statistical way – Standard uncertainty ~ **standard deviation** of variable **x**

- \Box probability density function (pdf) $p_X(x)$
- probability $Pr(x_1 \le X \le x_2) = \int_{x_1}^{x_2} p_X(x) dx$
- statistical mean $\overline{X} = \mu = \int_{-\infty}^{+\infty} x \cdot p_X(x) dx$
- statistical variance $\sigma^2 = \overline{(X \mu)^2} = \int_{-\infty}^{+\infty} (x \mu)^2 \cdot p_X(x) dx$
- standard deviation $\sigma = \sqrt{\sigma^2} = \sqrt{\overline{(X \mu)^2}}$

Gauss distribution (normal)

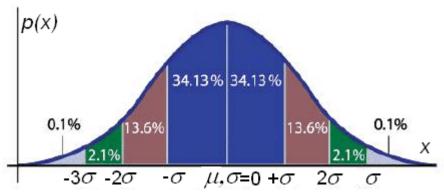
$$p_X(x) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right)$$

Standard deviation: σ

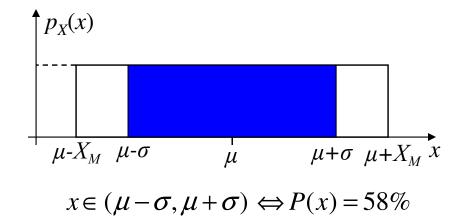
Uniform distribution

$$p_{X}(x) = \begin{cases} \frac{1}{2 \cdot X_{M}}, & x \in [\mu - X_{M}, \mu + X_{M}] \\ 0 & \text{otherwise} \end{cases}$$

Standard deviation $\sigma = \frac{X_M}{\sqrt{3}}$



Interval of x $(\mu \mp 0.6745 \cdot \sigma) \Leftrightarrow P(x) = 50.00\%$ $(\mu - \sigma, \mu + \sigma) \Leftrightarrow P(x) = 68.28\%$ $(\mu - 2\sigma, \mu + 2\sigma) \Leftrightarrow P(x) = 94.46\%$ $(\mu - 3\sigma, \mu + 3\sigma) \Leftrightarrow P(x) = 99.72\%$



Practical measurement accuracy

Evaluation from *N* samples (ergodic process supposition)

- ho error in the n-th measurement $e_{X_{-n}} = x_n \overline{X}$ $\varepsilon_{X_{-n}} = \frac{e_{X_{-n}}}{\overline{X}}$
- oxdot deviation of in the n-th measurement $e_{X_n} = x_n X$
- Average deviation $D_{X_N} = \frac{1}{N} \sum_{k=1}^{N} (x_k \overline{X})$

Practical measurement accuracy

Standard deviation (N>30)

$$\sigma_X = \sqrt{\frac{1}{N} \sum_{k=1}^{N} (x_k - \mu)^2}$$

Standard deviation (N<30)

$$\sigma_{X} = \sqrt{\frac{1}{N-1} \sum_{k=1}^{N} (x_{k} - \mu)^{2}}$$

Uncertainties propagation $Y = F(X_1, X_2, ..., X_K)$

$$Y = F(X_1, X_2, ..., X_K)$$

$$\sigma_{Y} = \sqrt{\sum_{k=1}^{K} \left(\frac{\partial F(X_{1}, X_{2}, ..., X_{K})}{\partial X_{k}} \right)^{2} \cdot \sigma_{X_{k}}^{2}}$$

Least mean squares linear fitting

Simplest case: one measurand is linear function of single independent variable

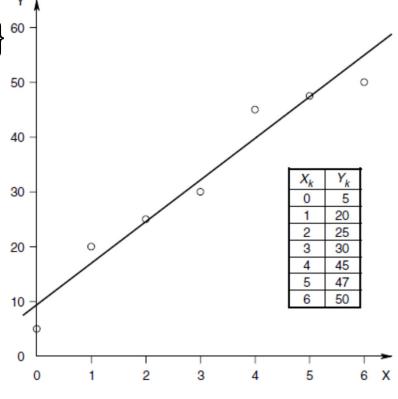
For N samples
$$X = \{x_1, x_2, ..., x_N\}^{60}$$

Linear fit
$$Y = \{y_1, y_2, ..., y_N\}$$

for every

$$\{y_n, x_n\}: \quad y_n = m \cdot x_n + b$$

Determine optimum m, b.



Least mean squares linear fitting

Minimize mean square error

$$MSE = \sigma_y^2 = \frac{1}{N} \sum_{n=1}^{N} ((m \cdot x_n + b) - y_n)^2$$

Set derivates equal to zero

$$\begin{cases} \frac{\partial \sigma_y^2}{\partial m} = 0 \\ \frac{\partial \sigma_y^2}{\partial b} = 0 \end{cases} \Rightarrow \begin{cases} m \cdot S_{xx} + b \cdot S_x = S_{xy} \\ m \cdot S_x + b \cdot N = S_y \end{cases}$$

where

$$S_{xx} = \sum_{n=1}^{N} x_n \cdot x_n \qquad ; \qquad S_x = \sum_{n=1}^{N} x_n$$

$$S_{xy} = \sum_{n=1}^{N} x_n \cdot y_n \qquad ; \qquad S_y = \sum_{n=1}^{N} y_n \quad ; \quad d = S_x^2 - N \cdot S_{xx}$$

Least mean squares linear fitting

- □ Solutions: $b = \frac{1}{d} \left(S_x \cdot S_{xy} S_y \cdot S_{xx} \right)$; $m = \frac{1}{d} \left(S_x \cdot S_y N \cdot S_{xy} \right)$
- $R_{xy}(0)$ cross correlogram function evaluated at t=0

$$R_{xy}(0) = \frac{1}{N} \sum_{n=1}^{N} x_n y_n = \frac{1}{N} S_{xy}$$

□ r - correlation coefficient for the LMS fit (goodness of the fit)

$$r \equiv \left[R_{xy}(0) - \overline{X} \overline{Y} \right] / \sigma_x \sigma_y, \ 0 \le r \le 1$$

r = 1 - perfect fit

 r^2 - coefficient of determination of the fit

- SI (System International Unit)
 - International Standard

Electric Current

- **.....**
- Fundamentals

Length	meter	m
Mass	kilometer	kg
Time	second	S
Temperature	degree Kelvin	°K
Luminous Intensity	candela	cd

ampere

Derived

	Electromotive Force	volt	\/
Ц	Electromotive Force	VOIL	V
	Quantity of Charge	coulomb	C
	Electrical Resistance	ohm	Ω
	Capacitance	farad	F
	Inductance	henry	Н

- Supplementary bibliography
 - S. Rabinovich, Measurement Errors and Uncertainties Theory and Practice 3rd ed. – 2005;
 - □ P.P.L. Regtien, Electronic instrumentation, second edition 2005;